

National Aeronautics and  
Space Administration

Jet Propulsion Laboratory  
California Institute of Technology  
Pasadena, California

# **GEOS-Chem Adjoint: Status from the Adjoint Working Group**

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**Jet Propulsion Laboratory**  
**California Institute of Technology**

**Joint Institute for Regional Earth System Science and Engineering**  
**University California, Los Angeles**



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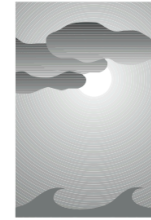
## GEOS-Chem Adjoint Working Group

- **The adjoint working group started in 2007 to coordinate adjoint development activities between several groups**
  - *Caltech*
  - *Harvard*
  - *Virginia Tech*
  - *Jet Propulsion Laboratory*
- **The number of active participants has increased**
  - *Caltech/ Columbia / NASA GISS / CU Boulder : **Daven Henze***
  - *Dalhousie: **Randall Martin, Chulkyu Lee***
  - *Harvard: **Monika Kopacz, Lin Zhang, Peter Zoogman, Daniel Jacob***
  - *JPL: **Kevin Bowman, Changsub Shim, Paul Hamer, Sunita Verma***
  - *UCLA: **Qinbin Li***
  - *U. of Toronto: **Dylan Jones, Mark Parrington, Michael Seymour, Thomas Walker***
  - *Virginia Tech: **Adrian Sandu, Kumaresh Singh, Paul Eller, Mohammed Jardak***



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# What Is an Adjoint Model?



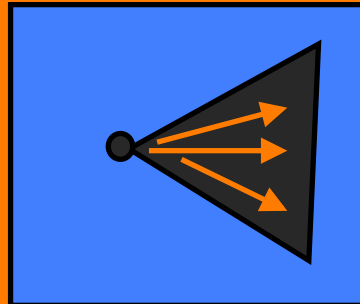
Ronald M. Errico  
National Center for Atmospheric Research,\* Boulder, Colorado

*BAMS*, 1997

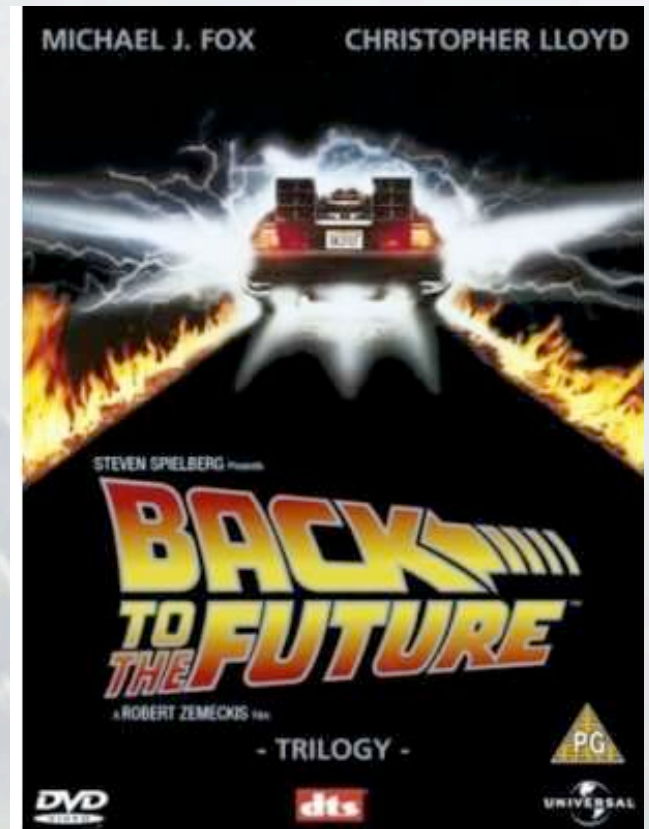
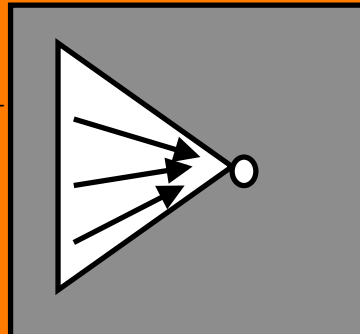
Let  $A$  be a bounded operator on a Hilbert Space,  $H$ .  
The adjoint operator is defined by:

$$A^* : H \rightarrow H \quad \langle Ax, y \rangle = \langle x, A^* y \rangle \quad \forall x, y \in E$$

$$\left( \frac{\partial \mathbf{x}^i}{\partial \mathbf{x}^0} \right)^\top = \left( \frac{\partial \mathbf{M}_{i-1}}{\partial \mathbf{x}_{i-1}} \cdots \frac{\partial \mathbf{M}_0}{\partial \mathbf{x}_0} \right)^\top$$



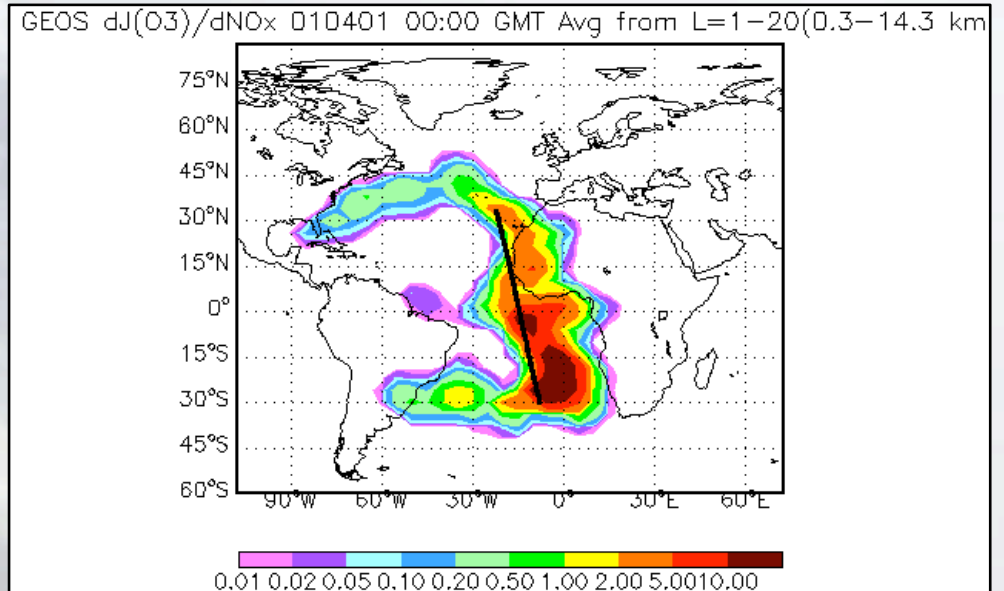
$$\left( \frac{\partial \mathbf{x}^i}{\partial \mathbf{x}^0} \right)^\top = \left( \frac{\partial \mathbf{M}_0}{\partial \mathbf{x}_0} \right)^\top \cdots \left( \frac{\partial \mathbf{M}_{i-1}}{\partial \mathbf{x}_{i-1}} \right)^\top$$



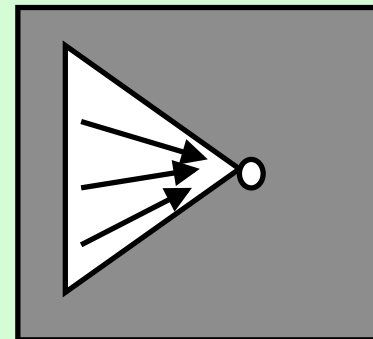


## Sensitivity Analysis

- Sensitivity of  $O_3$  along satellite track to global  $NO_x$  2 days prior
- Receptor-based approach, so time marches backwards
- Adjoints are at the heart of
  - 4D-variational source and state estimation
  - Sensitivity analysis
  - Stability/perturbation analysis



$$\left( \frac{\partial \mathbf{x}^i}{\partial \mathbf{x}^0} \right)^T = \left( \frac{\partial \mathbf{M}_0}{\partial \mathbf{x}_0} \right)^T \cdots \left( \frac{\partial \mathbf{M}_{i-1}}{\partial \mathbf{x}_{i-1}} \right)^T$$







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## Adjoint Model Status

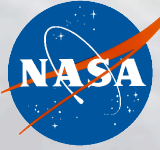
- **GEOS-Chem adjoint model versions:**
  - *GEOS-Chem v6-02-05, full chemistry with online aerosols (Henze-CU Boulder)*
  - *GEOS-Chem v6, tagged CO and Ox (Kopacz-Harvard)*
  - *GEOS-Chem v7, full chemistry (Singh-Virginia Tech)*
- **Versions described at**
  - *[http://wiki.seas.harvard.edu/geos-chem/index.php/GEOS-Chem\\_Adjoint](http://wiki.seas.harvard.edu/geos-chem/index.php/GEOS-Chem_Adjoint)*
  - *<http://filebox.vt.edu/~kumaresh/>*
  - *[http://spot.colorado.edu/~henzed/gc\\_adj.html/](http://spot.colorado.edu/~henzed/gc_adj.html/)*



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## GEOS-Chem v6-02-05, full chemistry with online aerosols

- **GEOS-3 and GEOS-4 met fields**
- **2x2.5, 4x5 model resolution**
- **OpenMP parallelized**
- **Observational Operators**
  - *IMPROVE PM2.5 (NO<sub>3</sub>, SO<sub>4</sub>, OC, BC)*
  - *CASTNet (NH<sub>4</sub><sup>+</sup>)*
  - *GOME / SCIAMACHY NO<sub>2</sub> column (KNMI and Dalhousie retrievals)*
  - *TES NH<sub>3</sub>*
- **Control parameters**
  - *Emissions scaling parameters (linear or log)*
    - SO<sub>x</sub>, NH<sub>3</sub>, primary BC/OC: anthro, natural, bioburn, biofuel, volcanoes
    - NO<sub>x</sub>: anthro, soil, lightning
  - *Initial concentration scaling factors (all, linear)*
- **Adjoint sensitivities**
  - *w.r.t control parameters*
  - *of AQ attainment metrics*
  - *of spatiotemporally averaged pollutant levels (e.g., arctic O<sub>3</sub>)*



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## GEOS-Chem v6-02-05 (builds on dkh version), tagged CO and Ox

- **GEOS-3, GEOS-4 met fields**
- **4x5, 2x2.5 model resolution**
- **OpenMP parallelized**
- **Observational Operators**
  - *MOPITT CO column*
  - *SCIAMACHY CO column using Bremen retrieval*
  - *AIRS CO column*
- **Control parameters**
  - *Emissions (CO)*
  - *Initial Conditions*
  - *Ox production*
- **Adjoint sensitivity analysis**
  - *w.r.t control parameters*



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## GEOS-Chem v7 with full chemistry

- **GEOS-4 met fields**
- **4x5 model, 2x2.5 resolution**
- **OpenMP parallelized**
- **Observational Operators**
  - *TES O3*
- **Control Parameters**
  - *Emissions scaling factors*
  - *Initial Conditions*
- **Adjoint sensitivity analysis w.r.t control parameters**





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## Adjoint Workshop goals

- **Adjoint model clinic (chairs: Kopacz, Singh, Henze)**
  - *Thurs. 11-12:30pm*
  - *Provide tutorials on adjoint usage with different model branches*
  - *Please sign-up at registration desk for interested participants*
- **Adjoint model development planning group (chairs: Bowman, Henze)**
  - *Thurs. 3:45- 5:15pm*
  - *Assess how/whether adjoint branches should be merged*
  - *Adjoint version releases relative to standard version releases*
  - *Migration to GEOS-5 v8*
  - *Next development milestones*
  - *Funding opportunities*
  - *Adjoint WG please sign up at registration desk*



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- **BACKUP**



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## Adjoint operator

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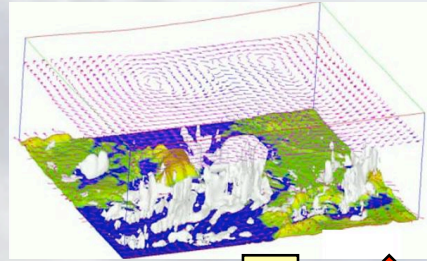
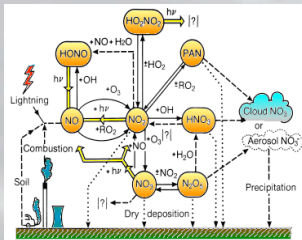


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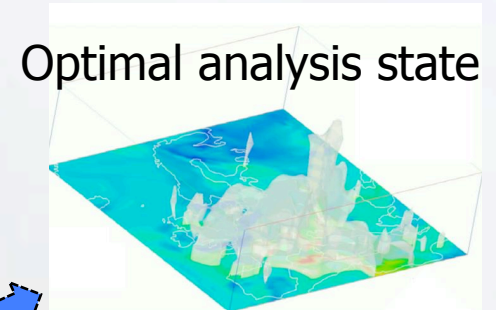
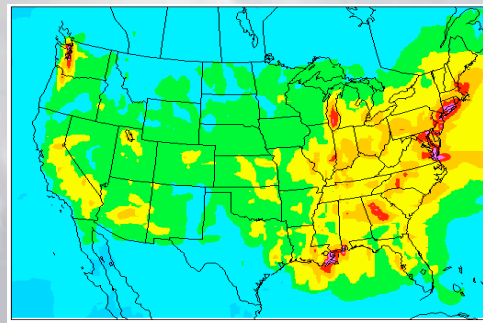
# Advancement in atmospheric chemistry through modeling, observations and assimilation

Transport  
 Meteorology

Chemical kinetics

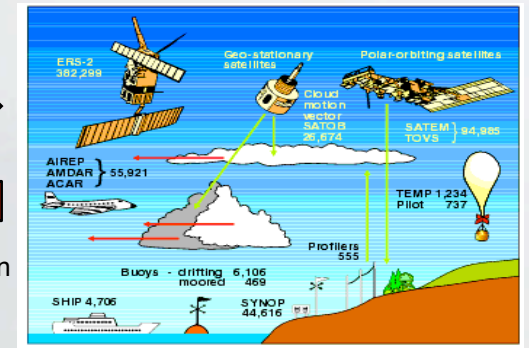


CTM

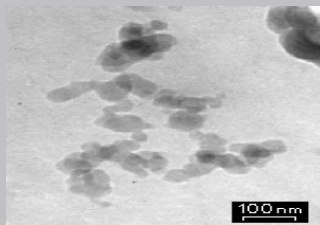


Optimal analysis state

Observations



Aerosols



Emissions



State/parameter estimation

$$\min_{\mathbf{x}_0} C(\mathbf{x}) = \left\{ \sum_i (\mathbf{y}_i - \mathbf{F}_i(\mathbf{x}))^\top (\mathbf{S}_n^i)^{-1} (\mathbf{y}_i - \mathbf{F}_i(\mathbf{x})) + (\mathbf{x}_0 - \mathbf{x}_a)^\top \mathbf{S}_a^{-1} (\mathbf{x}_0 - \mathbf{x}_a) \right\}$$

- We want to understand the sensitivity of ozone to processes
- We can observationally constrain parameters defined within those processes